

Recent Trends in Stochastic Analysis Special Session B21

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Stochastic analysis methods and robust techniques have recently led to a variety of advances in the theory of (stochastic) partial differential equations (PDEs). The spectrum of applications is very wide and includes stochastic homogenization, fluid mechanics, mathematical finance, statistical mechanics and the stochastic quantization of quantum field theories. The goal of the session is to bring together mathematicians who have applied stochastic analysis to (stochastic) PDEs of many different kinds, in particular singular stochastic PDEs such as KPZ and Φ^4 , Fisher-KPP PDE, Navier-Stokes PDE, and Stefan problems among others. The organizers are confident that such an exchange of ideas will lead to a number of further advances across different areas of (stochastic) PDEs.

For more information visit
umi.dm.unibo.it/jm-umi-ams/special-sessions/special-sessions-on-25-26-july-2024.

Schedule and Abstracts

July 25, 2024

11:30–12:10 TBA

Raluca Balan (University of Ottawa, CANADA)

Abstract. TBA

12:20–13:00 TBA

Giuseppe Cannizzaro (University of Warwick, UK)

Abstract. TBA

14:30–15:10 Limit laws in metric measure spaces

Maria Gordina (University of Connecticut, USA)

Abstract. We consider Dirichlet boundary problems in metric measure spaces. Results include properties of the spectrum, regularity and L^p -estimates of eigenfunctions, as well as irreducibility of the corresponding stochastic processes. A number of examples will be given including both local and non-local Dirichlet forms, hypoelliptic diffusions and stochastic processes on fractals, and applications to limit laws such as small deviations and large time behavior of the heat content.

15:20–16:00 TBA

Francesco Grotto (Università di Pisa, ITALY)

Abstract. TBA

17:00–17:40 TBA

Martin Hairer (École Polytechnique Fédérale de Lausanne, SWITZERLAND)

Abstract. TBA

July 26, 2024

11:30–12:10 TBA

Gautam Iyer (Carnegie Mellon University, USA)

Abstract. TBA

12:20–13:00 Fluctuations of Stochastic Heat Equation and KPZ equation

Xue-Mei Li (École Polytechnique Fédérale de Lausanne, SWITZERLAND)

Abstract. In this talk, we explore the stochastic heat equation and the KPZ equation, each influenced by space time Gaussian noise with long-range spatial dependence. These equations produce solutions that admit a stationary field. Our focus is on the fluctuation problem associated with diffusively scaled solutions from their average. While the behavior of compactly supported correlations—typically known to dissipate at large scales—is well-documented, our research shifts to examining long-range dependent noise with an asymptotic profile, inspired by empirical data and physical considerations. We investigate whether this dependence is maintained in the large-scale scaling limit. Our findings not only confirm its persistence but also reveal a key difference: the exponent in the power decay of the correlation rate plays a role akin to that of dimension in compactly supported scenarios. Furthermore, we demonstrate that the fluctuations of the appropriately scaled solutions from their mean converge weakly to the solution of a stochastic heat equation with additive noise, where the spatial correlation function is governed by the Riesz potential. In addressing the KPZ equation, we confront the challenges posed by the singular Cole-Hopf transformations. This research highlights the significance of long-range dependencies and their role in modeling more complex noise inputs in physical and mathematical models.

14:30–15:10 Cascade equation for Stefan problem as a mean field game

Sergey Nadtochiy (Illinois Institute of Technology, USA)

Abstract. The solutions to Stefan problem with Gibbs-Thomson law (i.e., with surface tension effect) are well known to exhibit singularities which, in particular, lead to jumps of the associated free boundary along the time variable. The correct times, directions and sizes of such jumps are only well understood under the assumption of radial symmetry, under which the free boundary is a sphere with varying radius. The characterization of such jumps in a general multidimensional setting has remained an open question until recently. In our ongoing work with M. Shkolnikov and Y. Guo, we have derived a separate (hyperbolic) partial differential equation — referred to as the cascade equation — whose solutions describe the jumps of the solutions to the Stefan problem without any symmetry assumptions. It turns out that a solution of the cascade equation corresponds to a maximal element of the set of all equilibria in a family of (first-order local) mean field games. In this talk, I will present and justify the cascade equation, will show its connection to the mean field games, and will prove the existence of a solution to the cascade equation. If time permits, I will also show how these results can be used to construct a solution to the Stefan problem itself.

15:20–16:00 TBA

Tommaso Rosati (University of Warwick, UK)

Abstract. TBA

17:00–17:40 TBA

Lenya Ryzhik (Stanford University, USA)

Abstract. TBA